# Statistical Analysis of Endorsement Experiments: Measuring Support for Militant Groups in Pakistan

Kosuke Imai

Department of Politics
Princeton University

Joint work with Will Bullock and Jacob Shapiro

May 6, 2011

# Motivation

- Survey is used widely in social sciences
- Validity of survey depends on the accuracy of self-reports
- Sensitive questions $\Longrightarrow$ social desirability, privacy concerns
  e.g., racial prejudice, corruptions
- Lies and nonresponses

- How can we elicit truthful answers to sensitive questions?
- Survey methodology: protect privacy through indirect questioning
- Statistical methodology: efficiently recover underlying responses

# Survey Techniques for Sensitive Questions

- Randomized Response Technique
  - Most extensively studied and commonly used
  - Use *randomization* to protect privacy
  - Difficulties: logistics, lack of understanding among respondents
- List Experiments
  - Also known as block total response and item count technique
  - Use *aggregation* to protect privacy
  - New estimators to enable *multivariate regression analysis*
  - New methods to detect and correct list experiment failures
- **Endorsement Experiments**
  - Use randomized *endorsements* to measure support levels
  - Develop a measurement model based on *item response theory*
  - Applications:
    1. Pakistanis' support for Islamic militant groups
    2. Afghanis' support for Taliban and ISAF (joint with J. Lyall)
    3. Nigerians' support for insurgents (joint with G. Blair)

# Endorsement Experiments

- Measuring support for political actors (e.g., candidates, parties) when studying sensitive questions
- Ask respondents to rate their support for a set of policies endorsed by randomly assigned political actors

- Experimental design:
  1. Select policy questions
  2. Randomly divide sample into control and treatment groups
  3. Across respondents and questions, randomly assign political actors for endorsement (no endorsement for the control group)
  4. Compare support level for each policy endorsed by different actors

# The Pakistani Survey Experiment

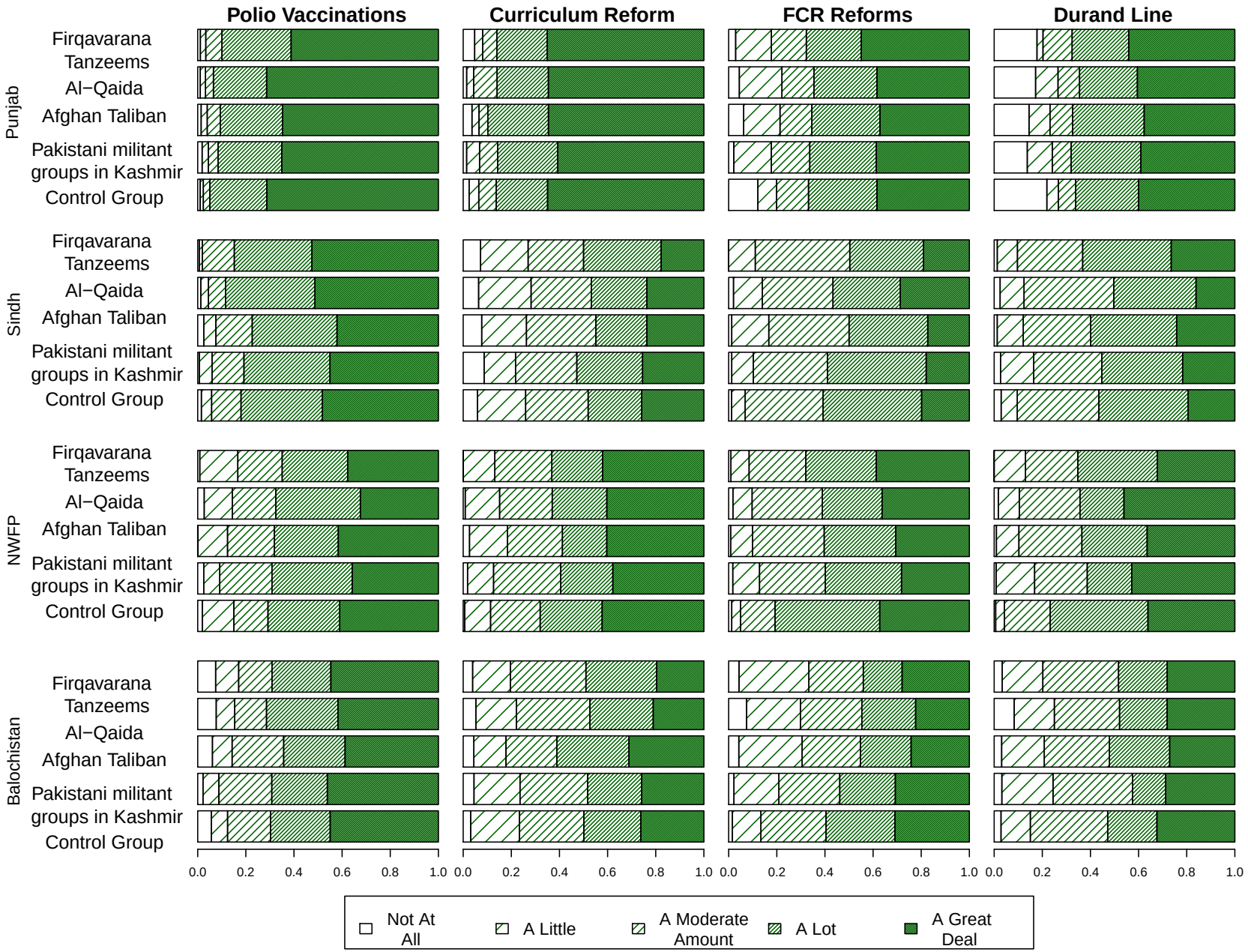
- 6,000 person urban-rural sample
- Four militant groups:
  - Pakistani militants fighting in Kashmir (a.k.a. Kashmiri tanzeem)
  - Militants fighting in Afghanistan (a.k.a. Afghan Taliban)
  - Al-Qa'ida
  - Firqavarana Tanzeems (a.k.a. sectarian militias)
- Four policies:
  - WHO plan to provide universal polio vaccination across Pakistan
  - Curriculum reform for religious schools
  - Reform of FCR to make Tribal areas equal to rest of the country
  - Peace jirgas to resolve disputes over Afghan border (Durand Line)
- Response rate over 90%

# Endorsement Experiment Questions: Example

- The script for the control group
- `The World Health Organization recently announced a plan to introduce universal Polio vaccination across Pakistan. How much do you support such a plan?`

- The script for the treatment group
- `The World Health Organization recently announced a plan to introduce universal Polio vaccination across Pakistan, a policy that has received support from Al-Qa'ida. How much do you support such a plan?`

# Distribution of Responses



# Methodological Challenges and Proposed Solutions

1. How to combine responses from multiple questions?
   $\Longrightarrow$ item response theory

2. How to recoup loss of statistical efficiency?
   $\Longrightarrow$ hierarchical modeling

3. What is the key assumption?
   $\Longrightarrow$ learning vs. support

4. How to select policy questions?
   - Policies should belong to a single dimension
   - Policies should be known to respondents
   - Respondents should not have strong views

# Endorsement Experiments Framework

- $N$ respondents
- $J$ policy questions
- $K$ political actors
- $Y_{ij} \in \{0, 1\}$: response of respondent $i$ to policy question $j$
- $T_{ij} \in \{0, 1, \ldots, K\}$: political actor randomly assigned to endorse policy $j$ for respondent $i$
- $Y_{ij}(t)$: potential response given the endorsement by actor $t$
- Covariates measured prior to the treatment

# The Proposed Model

- Quadratic random utility model:

$$\begin{aligned} U_i(\zeta_{j1}, k) &= -\|(x_i + s^*_{ijk}) - \zeta_{j1}\|^2 + \eta_{ij} \\ U_i(\zeta_{j0}, k) &= -\|(x_i + s^*_{ijk}) - \zeta_{j0}\|^2 + \nu_{ij} \end{aligned}$$

  where $x_i$ is the ideal point and $s^*_{ijk}$ is the "influence" of an endorsement

- The statistical model (item response theory):

$$\begin{aligned} \Pr(Y_{ij} = 1 \mid T_{ij} = k) &= \Pr(Y_{ij}(k) = 1) \\ &= \Pr(U_i(\zeta_{j1}, k) > U_i(\zeta_{j0}, k)) \\ &= \Pr(\alpha_j + \beta_j(x_i + s^*_{ijk}) > \epsilon_{ij}) \end{aligned}$$

- Support level: $\frac{\partial}{\partial s_{ijk}} \Pr(Y_{ij} = 1 \mid T_{ij} = k) > 0$ where

$$s_{ijk} = \begin{cases} s^*_{ijk} & \text{if } \beta_j \geq 0 \\ -s^*_{ijk} & \text{otherwise} \end{cases}$$

# The Proposed Model (Continued)

- Hierarchical modeling:

$$
\begin{aligned}
x_i &\overset{\text{indep.}}{\sim} \mathcal{N}(Z_i^\top \delta,\ \sigma_x^2) \\
s_{ijk} &\overset{\text{indep.}}{\sim} \mathcal{N}(Z_i^\top \lambda_{jk},\ \omega_{jk}^2) \\
\lambda_{jk} &\overset{\text{i.i.d.}}{\sim} \mathcal{N}(\theta_k, \Phi_k)
\end{aligned}
$$

- "Noninformative" hyper prior on $(\alpha_j, \beta_j, \delta, \theta_k, \omega_{jk}^2, \Phi_k)$

- Interpretation:
  - spacial model vs. factor analysis
  - learning vs. support

# Quantities of Interest and Model Fitting

- Average support level for each militant group $k$

$$\begin{aligned} \tau_{jk}(Z_i) &= Z_i^\top \lambda_{jk} \quad \text{for each policy } j \\ \kappa_k(Z_i) &= Z_i^\top \theta_k \quad \text{averaging over all policies} \end{aligned}$$

- Standardize them by dividing the (posterior) standard deviation of ideal points

- Bayesian Markov chain Monte Carlo algorithm
- Multiple chains to monitor convergence
- Implementation via `JAGS` (Plummer)

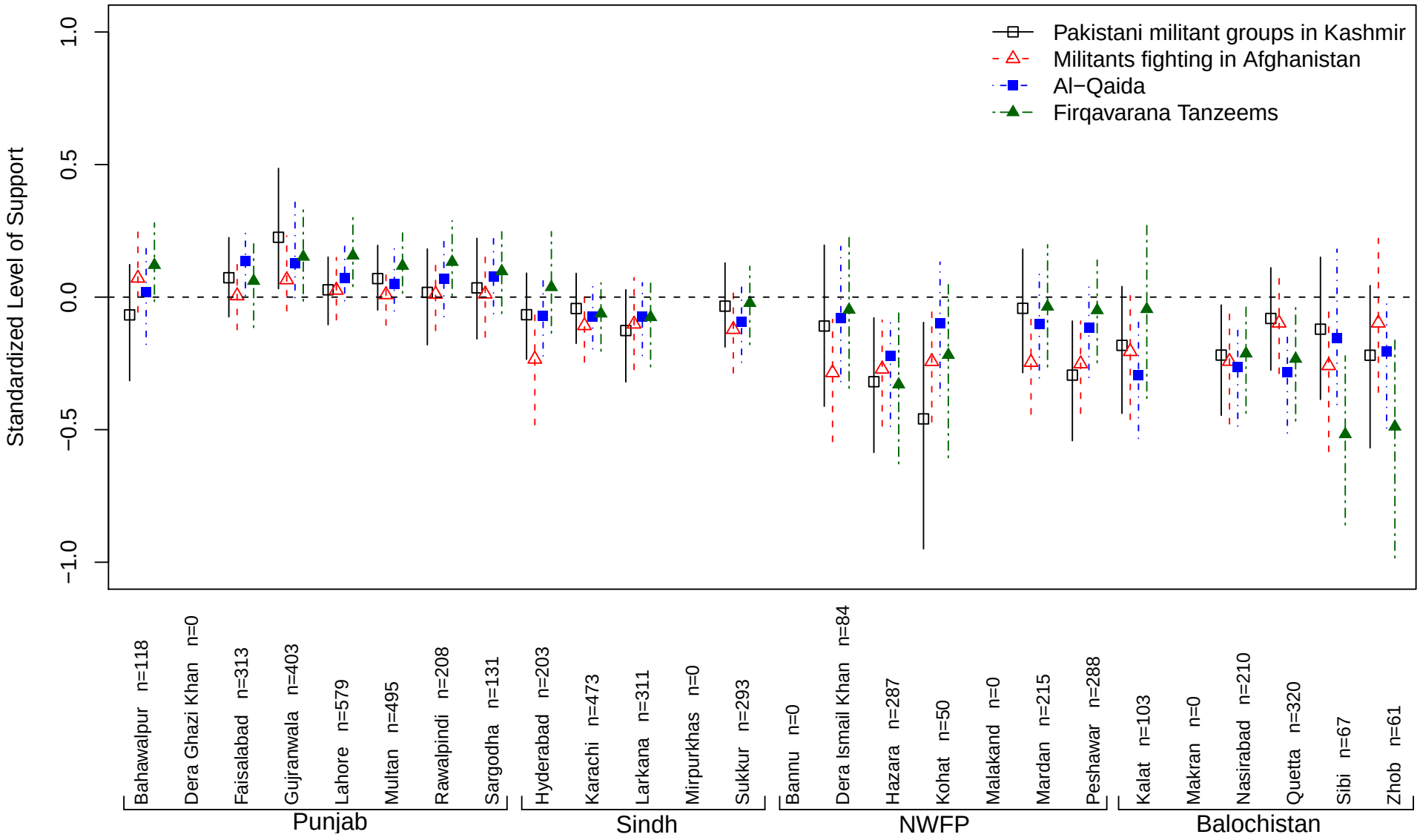
# Model for the Division Level Support

- Ordered response with an intercept $\alpha_{jl}$ varying across divisions
- The model specification:

$$
\begin{aligned}
x_i &\overset{\text{indep.}}{\sim} \mathcal{N}(\delta_{\text{division}[i]}, 1) \\
s_{ijk} &\overset{\text{indep.}}{\sim} \mathcal{N}(\lambda_{k,\text{division}[i]}, \omega_k^2) \\
\delta_{\text{division}[i]} &\overset{\text{indep.}}{\sim} \mathcal{N}(\mu_{\text{province}[i]}, \sigma^2_{\text{province}[i]}) \\
\lambda_{k,\text{division}[i]} &\overset{\text{indep.}}{\sim} \mathcal{N}(\theta_{k,\text{province}[i]}, \Phi_{k,\text{province}[i]})
\end{aligned}
$$

- Averaging over policies
- Partial pooling across divisions within each province

# Estimated Division Level Support



# Model with Individual Covariates

- Ordered response with an intercept $\alpha_{jl}$ varying across divisions
- The model specification:

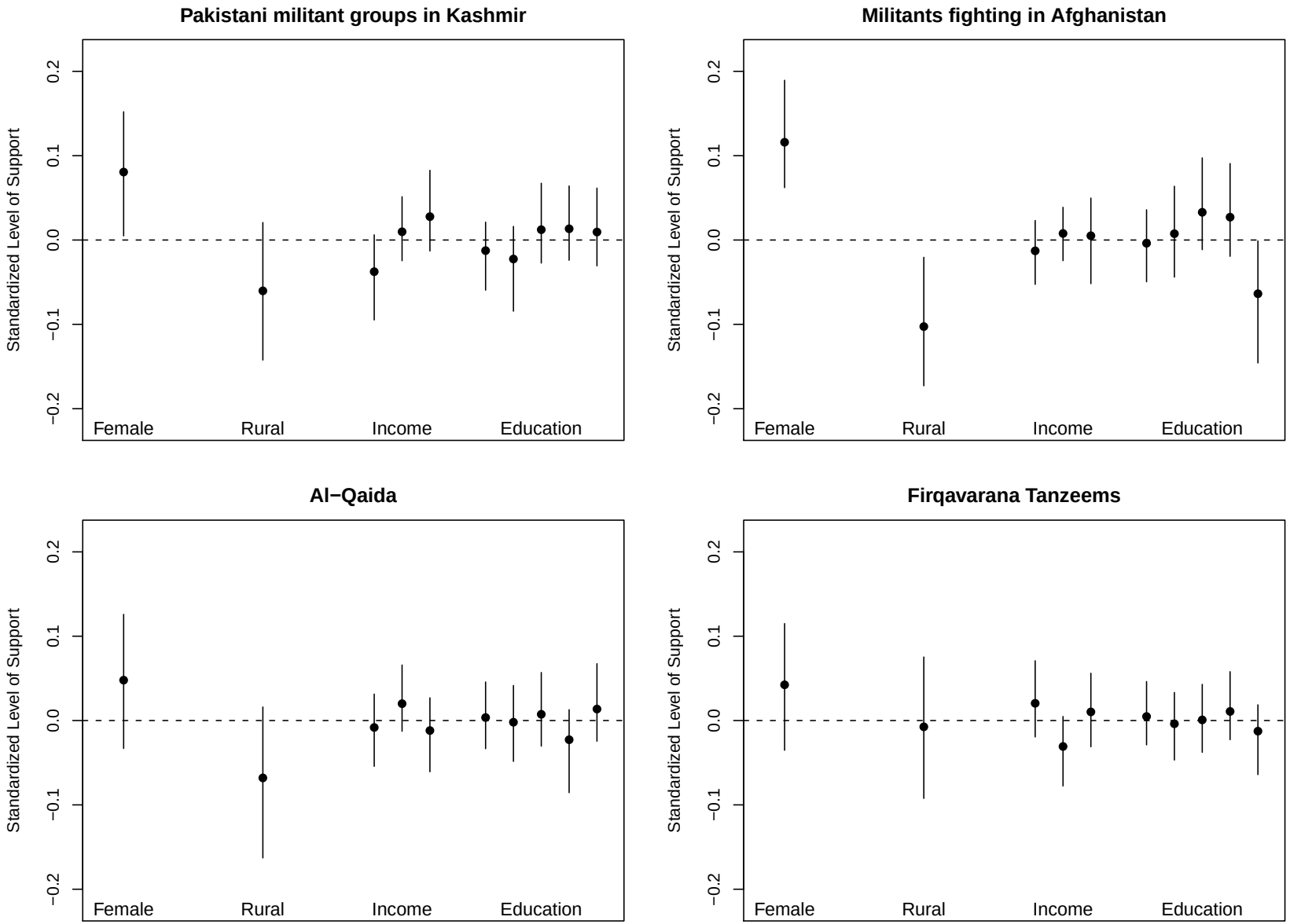
$$
\begin{aligned}
x_i &\overset{\text{indep.}}{\sim} \mathcal{N}(\delta_{\text{division}[i]} + Z_i^\top \delta^Z, 1) \\
s_{ijk} &\overset{\text{indep.}}{\sim} \mathcal{N}(\lambda_{k,\text{division}[i]} + Z_i^\top \lambda_k^Z, \omega_k^2) \\
\delta_{\text{division}[i]} &\overset{\text{indep.}}{\sim} \mathcal{N}(\mu_{\text{province}[i]}, \sigma^2_{\text{province}[i]}) \\
\lambda_{k,\text{division}[i]} &\overset{\text{indep.}}{\sim} \mathcal{N}(\theta_{k,\text{province}[i]}, \Phi_{k,\text{province}[i]})
\end{aligned}
$$

- Expands upon the division level model to include individual level covariates:

  gender, urban/rural, education, income

- Individual level covariate effects after accounting for differences across divisions
- Poststratification on these covariates using the census

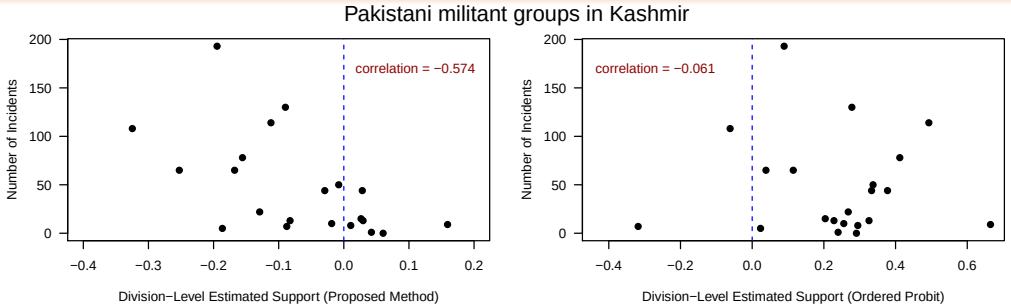
# Estimated Effects of Individual Covariates

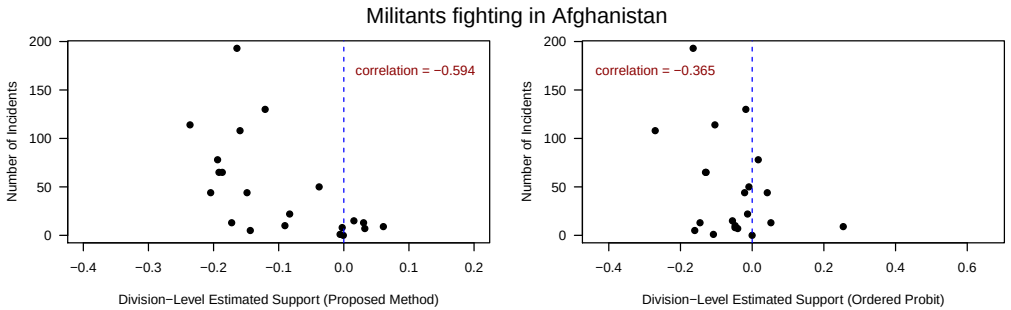


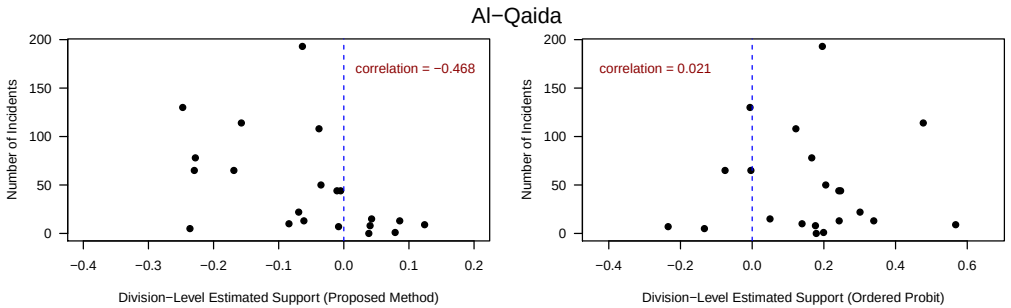

- Demographics play a small role in explaining support for groups

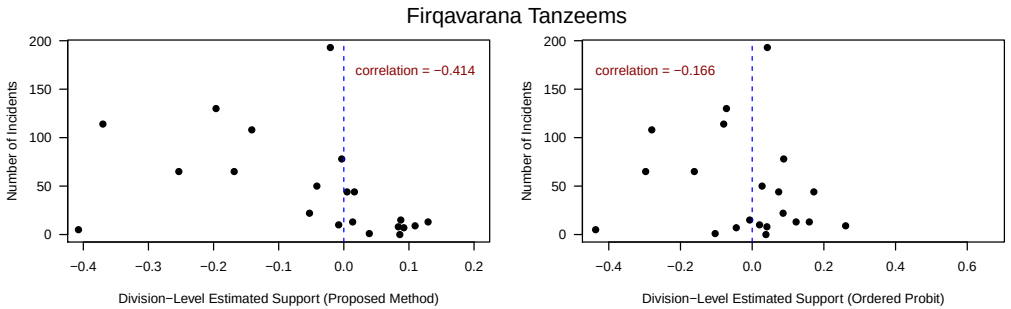
# Regional Clustering of the Support for Al-Qaida

# Association between Support and Violence



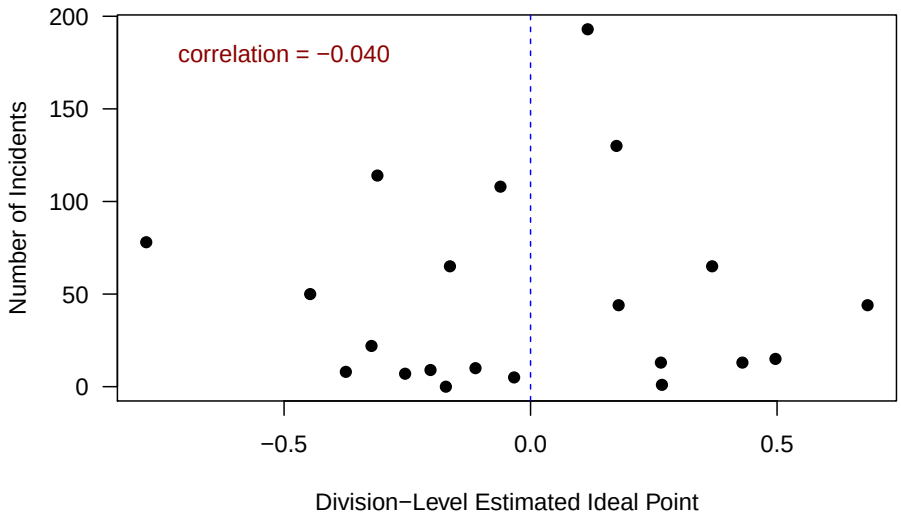



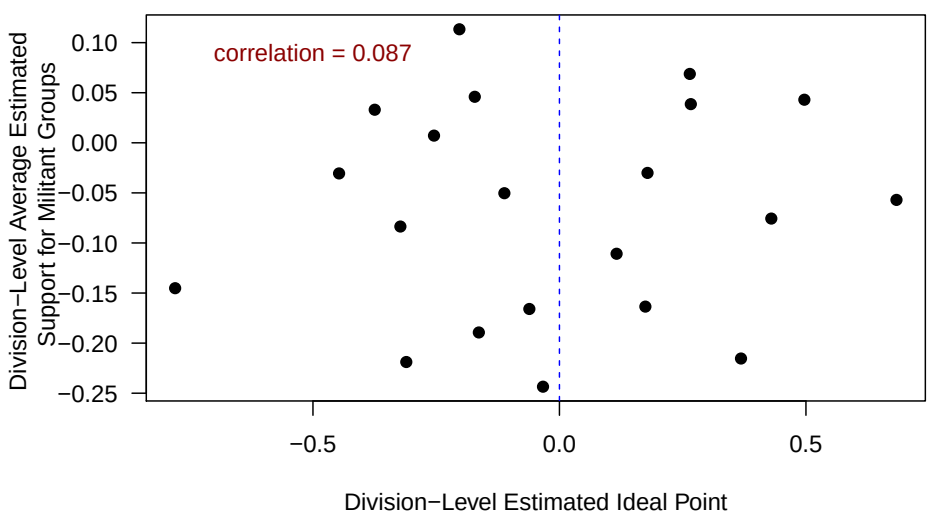




- Strong negative association between support and violence
- Much weaker association for the standard ordered probit model (division dummies, treatment variables interacted with division dummies)

# Ideology, Support, and Violence

- No strong relationship between:
  - ideology and violence
  - ideology and support



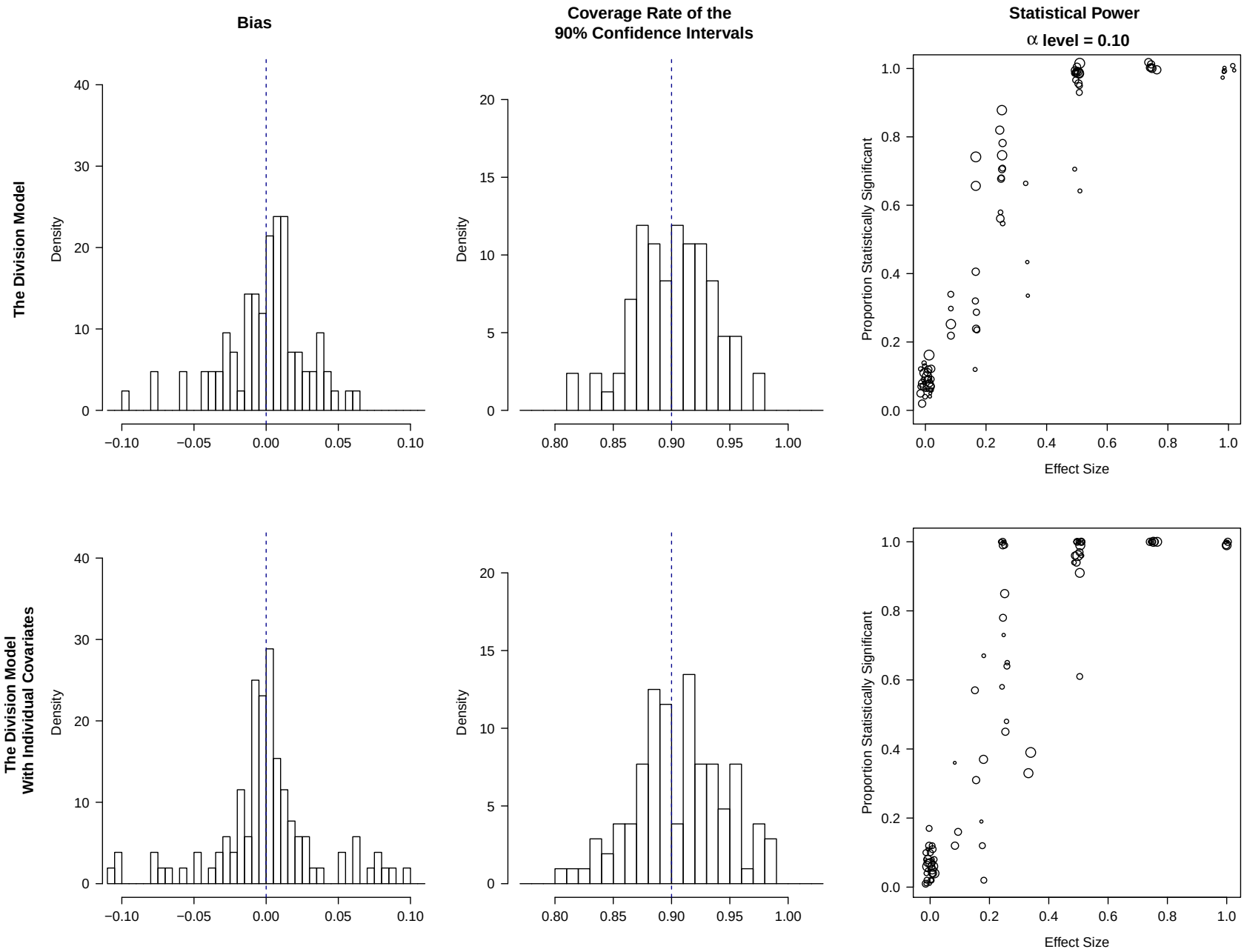



# Simulation Studies

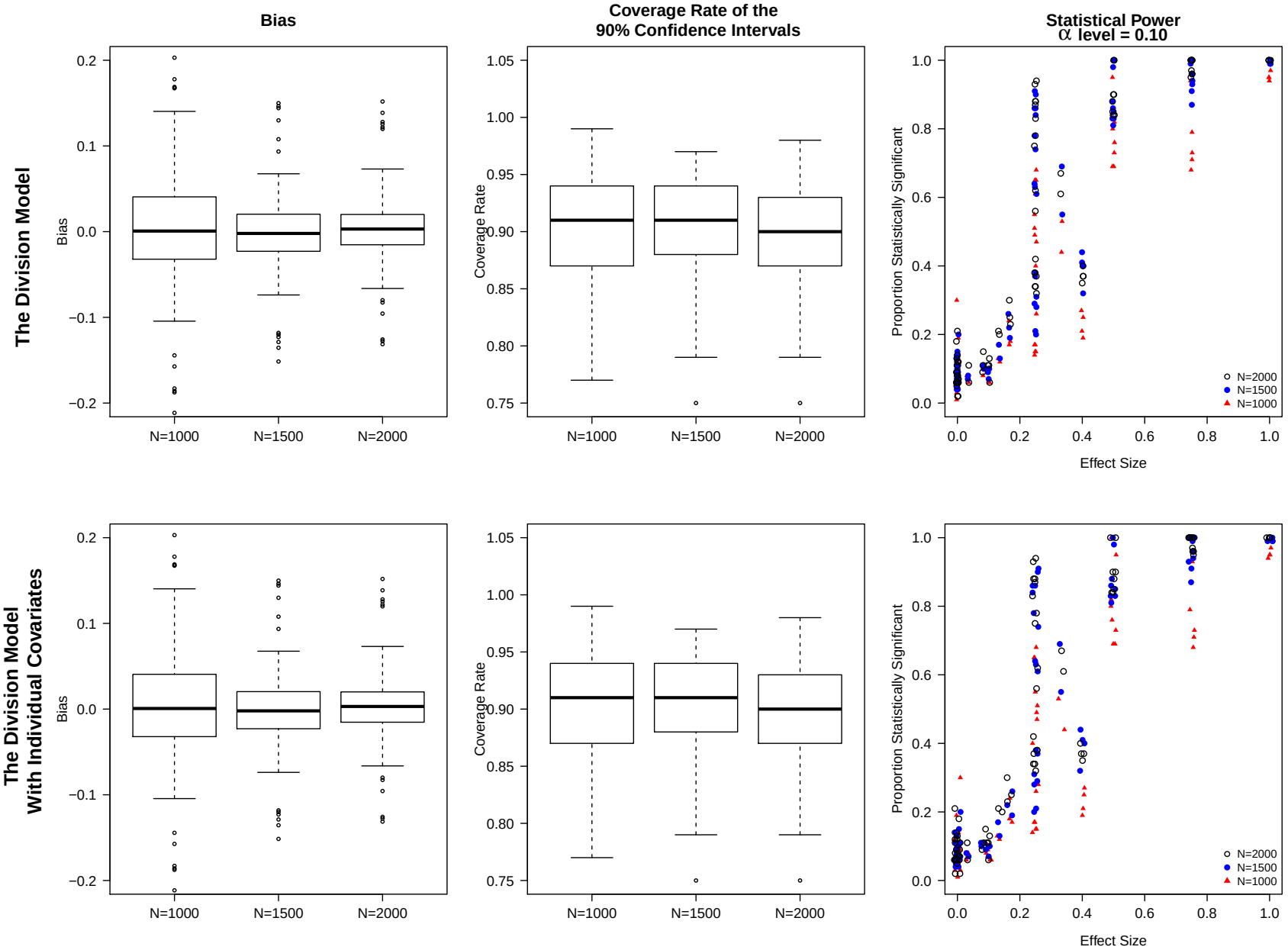
1. Based on the Pakistani Data
   - Same 2 models plus province-level issue ownership model
   - Top-level parameters held constant across simulations
   - Sample sizes and distribution same as before
   - Ideal points, endorsements and responses follow IRT models
2. Varying sample sizes
   - Model for division-level estimates with no covariates
   - Model for province-level estimates with no covariates but support varying across policies
   - $N = 1000, 1500, 2000$
   - Again, top-level parameters held constant across simulations while ideal points, endorsements and responses follow IRT models

- 100 simulations under each scenario (3 chains, 60000 iterations)
- Frequentist evaluation of Bayesian estimators

# Monte Carlo Evidence based on the Pakistani Data



# Monte Carlo Evidence with Varying Sample Size



# Concluding Remarks

- Survey methodology to study sensitive questions
- Endorsement Experiments
  - Most indirect form of questioning
  - Applicability limited to measuring support
  - Analysis based on the ideal points framework
  - Multilevel modeling to efficient estimation of spatial patterns
- Design considerations:
  - Policy positions should not be well-known
  - Response distribution should not be skewed
  - Policies should belong to a single dimension
  - Measure policy positions and political knowledge separately