Statistical Analysis of Endorsement Experiments: Measuring Support for Militant Groups in Pakistan

Kosuke Imai

Department of Politics Princeton University

Joint work with Will Bullock and Jacob Shapiro

May 13, 2011

- Survey is used widely in social sciences
- Validity of survey depends on the accuracy of self-reports
- Sensitive questions ⇒ social desirability, privacy concerns e.g., racial prejudice, corruptions
- Lies and nonresponses
- How can we elicit truthful answers to sensitive questions?
- Survey methodology: protect privacy through indirect questioning
- Statistical methodology: efficiently recover underlying responses

Survey Methodologies for Sensitive Questions

• Randomized Response Technique

- Most extensively studied
- Use randomization to protect privacy
- Difficulties: logistics, lack of understanding among respondents
- List Experiments (item count technique)
 - Use aggregation to protect privacy
 - New multivariate regression analysis method
 - New methods to detect and correct failures (joint with G. Blair)
 - Difficulties: design effects, ceiling and floor effects

- Use randomized endorsements to measure support levels
- Develop a measurement model based on item response theory
- Difficulties: interpretation, need for modeling
- Applications:
 - 0
 - Pakistanis' support for Islamic militant groups
 - Afghanis' support for Taliban and ISAF (joint with J. Lyall)
 - Nigerians' support for insurgents (joint with G. Blair)

- Measuring support for political actors (e.g., candidates, parties) when studying sensitive questions
- Ask respondents to rate their support for a set of policies endorsed by randomly assigned political actors
- Experimental design:
 - Select policy questions
 - Pandomly divide sample into control and treatment groups
 - Across respondents (and questions), randomly assign political actors for endorsement (no endorsement for the control group)
 - Compare support level for each policy endorsed by different actors

The Pakistani Survey Experiment

- 6,000 person urban-rural sample in April 2009
- Four militant groups:
 - Pakistani militants fighting in Kashmir (a.k.a. Kashmiri tanzeem)
 - Militants fighting in Afghanistan (a.k.a. Afghan Taliban)
 - Al-Qa'ida
 - Firqavarana Tanzeems (a.k.a. sectarian militias)
- Four policies:
 - WHO plan to provide universal polio vaccination across Pakistan
 - Curriculum reform for religious schools
 - Reform of FCR to make Tribal areas equal to rest of the country
 - Peace jirgas to resolve disputes over Afghan border (Durand Line)
- Response rate over 90%

• The script for the control group

The World Health Organization recently announced a plan to introduce universal Polio vaccination across Pakistan. How much do you support such a plan?

(1) A great deal (2) A lot (3) A moderate amount

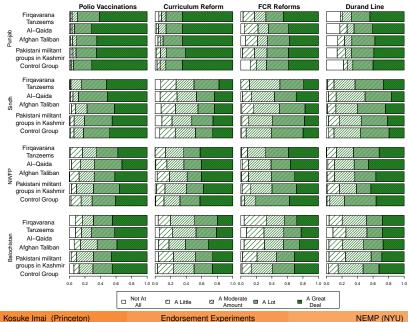
(4) A little (5) Not at all

• The script for a treatment group

The World Health Organization recently announced a plan to introduce universal Polio vaccination across Pakistan, a policy that has received support from Al-Qa'ida. How much do you support such a plan?

(1) A great deal (2) A lot (3) A moderate amount(4) A little (5) Not at all

Distribution of Responses



NEMP (NYU) 7/24

Methodological Challenges and Proposed Solutions

- How to combine responses from multiple questions? item response theory
- Observe the second second
- How to interpret the "support"? \implies policy vs. valence
- How to select policy questions?
 - Policies should belong to a single dimension
 - Respondents should not have strong views
 - Should one use well-known policies?: Statistical and substantive tradeoffs

- N respondents
- J policy questions
- K political actors
- $Y_{ij} \in \{0, 1\}$: response of respondent *i* to policy question *j*
- *T_{ij}* ∈ {0, 1, ..., *K*}: political actor randomly assigned to endorse policy *j* for respondent *i*
- $Y_{ij}(t)$: potential response given the endorsement by actor t
- Covariates measured prior to the treatment

The Proposed Model

• Quadratic random utility model (Clinton, Jackman, and Rivers):

$$U_{i}(\zeta_{j1}, k) = -\|(x_{i} + s_{ijk}^{*}) - \zeta_{j1}\|^{2} + \eta_{ij}$$

$$U_{i}(\zeta_{j0}, k) = -\|(x_{i} + s_{ijk}^{*}) - \zeta_{j0}\|^{2} + \nu_{ij}$$

 x_i is the ideal point and s_{ijk}^* is the "influence" of endorsement

• The statistical model (item response theory):

$$\begin{aligned} \mathsf{Pr}(Y_{ij} = 1 \mid T_{ij} = k) &= \mathsf{Pr}(Y_{ij}(k) = 1) \\ &= \mathsf{Pr}(U_i(\zeta_{j1}, k) > U_i(\zeta_{j0}, k)) \\ &= \mathsf{Pr}(\alpha_j + \beta_j(x_i + \mathbf{s}_{ijk}^*) > \epsilon_{ij}) \end{aligned}$$

• Support level: greater support \iff greater prob. of $Y_{ij} = 1$

$$m{s}_{ijk} = \left\{egin{array}{cc} m{s}_{ijk}^* & ext{if } eta_j \geq 0 \ -m{s}_{ijk}^* & ext{otherwise} \end{array}
ight.$$

The Proposed Model (Continued)

• Hierarchical modeling:

$$\begin{array}{lll} x_i & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(Z_i^{\top}\delta, \ \sigma_x^2) \\ s_{ijk} & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(Z_i^{\top}\lambda_{jk}, \ \omega_{jk}^2) \\ \lambda_{jk} & \stackrel{\mathrm{i.i.d.}}{\sim} & \mathcal{N}(\theta_k, \Phi_k) \end{array}$$

- "Noninformative" hyper prior on $(\alpha_j, \beta_j, \delta, \theta_k, \omega_{jk}^2, \Phi_k)$
- Interpretation:
 - spacial model vs. factor analysis
 - policy vs. valence aspects of support

Average support level for each militant group k

$$\tau_{jk}(Z_i) = Z_i^{\top} \lambda_{jk}$$
 for each policy j
 $\kappa_k(Z_i) = Z_i^{\top} \theta_k$ averaging over all policies

- Standardize them by dividing the (posterior) standard deviation of ideal points
- Bayesian Markov chain Monte Carlo algorithm
- Multiple chains to monitor convergence
- Implementation via JAGS (Plummer)

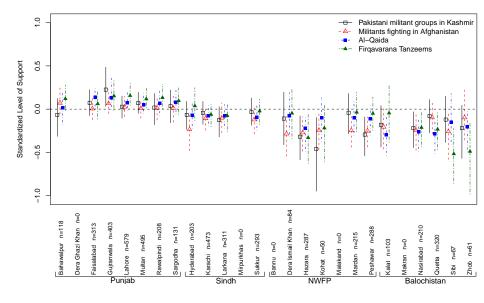
Model for the Division Level Support

Ordered response with an intercept *α_{jl}* varying across divisions
The model specification:

$$\begin{array}{cccc} x_i & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(\delta_{\mathrm{division}[i]}, \mathbf{1}) \\ & \mathbf{S}_{ijk} & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(\lambda_{k,\mathrm{division}[i]}, \omega_k^2) \\ & \delta_{\mathrm{division}[i]} & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(\mu_{\mathrm{province}[i]}, \sigma_{\mathrm{province}[i]}^2) \\ & \lambda_{k,\mathrm{division}[i]} & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(\theta_{k,\mathrm{province}[i]}, \Phi_{k,\mathrm{province}[i]}) \end{array}$$

- Averaging over policies
- Partial pooling across divisions within each province

Estimated Division Level Support



Model with Individual Covariates

Ordered response with an intercept *α_{jl}* varying across divisions
The model specification:

$$\begin{array}{rcl} x_i & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(\delta_{\mathrm{division}[i]} + Z_i^{\top} \delta^Z, \mathbf{1}) \\ \mathbf{s}_{ijk} & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(\lambda_{k,\mathrm{division}[i]} + Z_i^{\top} \lambda_k^Z, \omega_k^2) \\ \delta_{\mathrm{division}[i]} & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(\mu_{\mathrm{province}[i]}, \sigma_{\mathrm{province}[i]}^2) \\ \lambda_{k,\mathrm{division}[i]} & \stackrel{\mathrm{indep.}}{\sim} & \mathcal{N}(\theta_{k,\mathrm{province}[i]}, \Phi_{k,\mathrm{province}[i]}) \end{array}$$

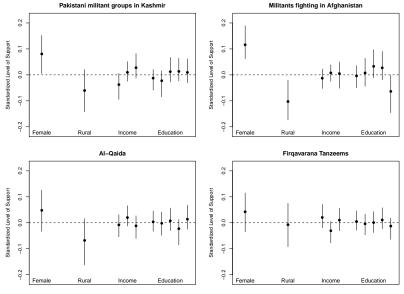
• Expands upon the division level model to include individual level covariates:

gender, urban/rural, education, income

- Individual level covariate effects after accounting for differences across divisions
- Poststratification on these covariates using the census

Kosuke Imai (Princeton)

Estimated Effects of Individual Covariates



• Demographics play a small role in explaining support for groups

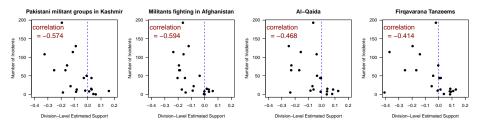
Regional Clustering of the Support for Al-Qaida



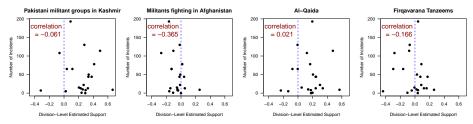
- Comparison with the "knowledge on the ground"
 - Greatest support in Punjab: consistent
 - Support in Gujranwala but not in Bahawalpur: surprising (US AID?)
- Least tolerant where senior leadership resides
 - Hazara for Al-Qa'ida
 - Quetta and Zhob for Taliban
- Least support where many terrorist attacks before April 2009
 - Hazara, Kohat, Nasirabad, Peshawar, and Quetta all suffered from attacks in early 2009
 - Data on "politically motivated violence" from March 2008 through March 2009 (National Counterterrorism Center's Worldwide Incident Tracking System)

Association between Support and Violence

• Strong negative association



 Weaker association for the standard ordered probit model (division dummies, treatment variables, their interactions)

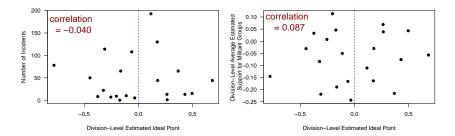


Kosuke Imai (Princeton)

Ideology, Support, and Violence

• No strong relationship between:

- ideology and violence
- ideology and support



Simulation Studies



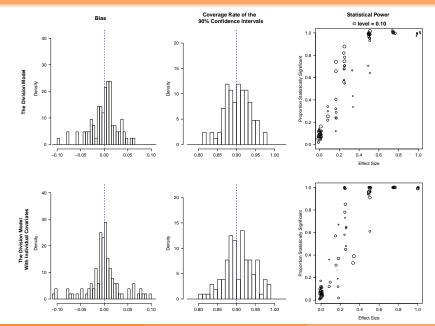
Based on the Pakistani Data

- Same 2 models plus province-level issue ownership model
- Top-level parameters held constant across simulations
- Sample sizes and distribution same as before
- Ideal points, endorsements and responses follow IRT models

2 Varying sample sizes

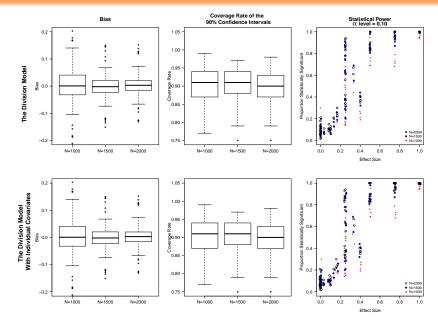
- Model for division-level estimates with no covariates
- Model for province-level estimates with no covariates but support varying across policies
- *N* = 1000, 1500, 2000
- Again, top-level parameters held constant across simulations while ideal points, endorsements and responses follow IRT models
- 100 simulations under each scenario (3 chains, 60000 iterations)
- Frequentist evaluation of Bayesian estimators

Monte Carlo Evidence based on the Pakistani Data



Kosuke Imai (Princeton)

Monte Carlo Evidence with Varying Sample Size



Kosuke Imai (Princeton)

Concluding Remarks

• Survey methodology to study sensitive questions

- Most indirect form of questioning
- Applicability limited to measuring support
- Analysis based on the item response framework
- Multilevel modeling to efficient estimation of spatial patterns
- Design considerations:
 - Policies should belong to a single dimension
 - Respondents should not have strong opinion
 - · Separating policy and valence aspects of support
 - Statistical vs. substantive tradeoffs
 - Could measure policy positions and political knowledge separately
- JAGS code available at the dataverse